Option Volatility and Pricing

Advanced Trading Strategies and Techniques

SECOND EDITION

SHELDON NATENBERG



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