

The Capital Asset Pricing Model
in the 21st Century

*Analytical, Empirical, and Behavioral
Perspectives*

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