

Commodities and Commodity Derivatives

Modeling and Pricing for Agriculturals,
Metals and Energy

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